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**Definition:** The **Dirac delta “function”** is  $\delta(t - t_0) = \lim_{a \rightarrow 0} \delta_a(t - t_0)$ .

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**Theorem:** Transform of the Dirac Delta Function

For  $t_0 > 0$ ,  $\mathcal{L} \{ \delta(t - t_0) \} = e^{-st_0}$ .

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Note that when  $t_0 = 0$ , we have  $\mathcal{L}\{\delta(t)\} = 1$ .

**Example:** Use the Laplace transform to solve the given initial-value problem.

$$y'' + y = \delta(t - 2\pi) + \delta(t - 4\pi), \quad y(0) = 1, \quad y'(0) = 0$$

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$$y'' - 7y' + 6y = e^t + \delta(t - 2) + \delta(t - 4), \quad y(0) = 0, \quad y'(0) = 0$$

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